## AQA

# A-LEVEL <br> Mathematics 

Statistics 1B - MS1B
Mark scheme

6360
June 2015

Version/Stage: 1.0: Final

Mark schemes are prepared by the Lead Assessment Writer and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all associates participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the students' responses to questions and that every associate understands and applies it in the same correct way. As preparation for standardisation each associate analyses a number of students' scripts: alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, associates encounter unusual answers which have not been raised they are required to refer these to the Lead Assessment Writer.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of students' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

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## Key to mark scheme abbreviations

| M | mark is for method |
| :--- | :--- |
| m or dM | mark is dependent on one or more M marks and is for method |
| A | mark is dependent on M or m marks and is for accuracy |
| B | mark is independent of M or m marks and is for method and accuracy |
| E | mark is for explanation |
| Jor ft or F | follow through from previous incorrect result |
| CAO | correct answer only |
| CSO | correct solution only |
| AWFW | anything which falls within |
| AWRT | anything which rounds to |
| ACF | any correct form |
| AG | answer given |
| SC | special case |
| OE | or equivalent |
| A2,1 | 2 or 1 (or 0 ) accuracy marks |
| $-x$ EE | deduct $x$ marks for each error |
| NMS | no method shown |
| PI | possibly implied |
| SCA | substantially correct approach |
| c | candidate |
| $s f$ | significant figure(s) |
| dp | decimal place(s) |

## No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award full marks. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn no marks.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns full marks, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains no marks.

Otherwise we require evidence of a correct method for any marks to be awarded.

## General Notes for MS1B

GN1 There is no allowance for misreads (MR) or miscopies (MC) unless specifically stated in a question
GN2 In general, a correct answer (to accuracy required) without working scores full marks but an incorrect answer (or an answer not to required accuracy) scores no marks

GN3 When applying AWFW, a slightly inaccurate numerical answer that is subsequently rounded to fall within the accepted range cannot be awarded full marks.

GN4 Where percentage equivalent answers are permitted in a question, then penalise by one accuracy mark at the first correct answer but only if no indication of percentage (eg \%) is shown

GN5 In questions involving probabilities, do not award accuracy marks for answers given in the form of a ratio or odds such as $11 / 30$ given as 11:30 or 11:19

GN6 Accept decimal answers, providing that they have at least two leading zeros, in the form $c \times 10^{-n}$ (eg 0.00524 as $5.24 \times 10^{-3}$ )

| Q | Solution | Marks | Total | Comments |
| :---: | :---: | :---: | :---: | :---: |
| $\begin{gathered} 1 \\ \text { (a) } \end{gathered}$ | Using summary data with shown method: $\begin{aligned} r_{x y}=\frac{3629670}{\sqrt{76581640 \times 694250}} & \\ & =\underline{\mathbf{0 . 4 9} \text { to } 0.5} \end{aligned}$ | M1 <br> A1 |  | Used; accept (all 3 values) $\div 10$ Can be implied by a correct answer <br> AWFW <br> (0.497791) |
|  | Using summary data without shown method or using raw data with or without shown method: $\begin{aligned} & r_{x y}=\underline{0.49 \text { to } 0.5} \\ & r_{x y}=\underline{0.4 \text { to } 0.6} \end{aligned}$ | (B2) (B1) | 2 | AWFW AWFW |
| (b) | Moderate/some <br> positive (linear) correlation <br> between <br> gas and electricity consumptions | Bdep1 <br> B1 | 2 | Dependent on $\mathbf{0 . 4} \leq \boldsymbol{r}_{\boldsymbol{x y}} \leq \mathbf{0 . 6}$ <br> OE; must qualify strength and state positive <br> Providing $\mathbf{- 1}<\boldsymbol{r}_{x y}<+\mathbf{1}$ OE; must be in context |
| Notes | 1 Only accept phrases stated; ignore additional comments unless contradictory <br> 2 Use of any of the following terms (even in conjunction with moderate/some): "strong or high or big or good or low or little or small or weak or slight or medium or average or reasonable or pretty" $\Rightarrow$ Bdep0 <br> 3 Accept "relationship/association/link" but not "trend" instead of "correlation" <br> 4 As gas consumption increases then electricity consumption increases $\Rightarrow$ Bdep0 B1 <br> 5 Do not accept "between $x$ and $y$ " or "between kWh" or "between consumptions" or "between gas and electricity" without further clarification |  |  |  |
|  |  | Total | 4 |  |


| Q | Solution | Marks | Total | Comments |
| :---: | :---: | :---: | :---: | :---: |
| $\begin{gathered} \mathbf{2} \\ \text { (a) } \end{gathered}$ | ```Mid-points (d): \(\begin{array}{lllllll}65.5 & 66.5 & 67.5 & 68.5 & 69.5 & 70.5 & 71.5\end{array}\) Mean \(=\underline{68.2 \text { to } 68.3}\) \(\operatorname{Var}(n)=\underline{\mathbf{2 . 4 2}}\) or \(\operatorname{Var}(n-1)=\underline{\mathbf{2 . 4 6}}\) or \(\operatorname{Var}(n)\) or \(\operatorname{Var}(n-1)=\underline{\mathbf{2} .4 \text { to } 2.5}\)``` | M1 <br> A1 <br> B2 <br> (B1) | 4 | At least four seen or implied (only) from $\sum f d=4095$ <br> or mean $=68.2$ to 68.3 AWFW or mean $=68.5 \mathrm{CAO}$ <br> AWFW <br> (68.25) <br> (2.42083) <br> AWRT $\left(\sum f d^{2}=279629\right)$ <br> (2.46186) <br> AWFW |
| Notes | $\begin{aligned} & \mathbf{1} \text { Value of variance stated as } 1.55^{2} \text { to } 1.57^{2} \text { and not evaluated } \Rightarrow \mathrm{B} 1 \\ & \mathbf{2} \text { Value of variance or standard deviation stated as } 1.55 \text { to } 1.57 \Rightarrow \mathrm{~B} 0 \\ & \mathbf{3} \text { If, and only if, M0 A0 B0, then award M1 for seen attempt at } \sum f \times(d / L C B / U C B) \div 60 \text { or }(4095 / 4065 / 4125) \div 60 \\ & \hline \end{aligned}$ |  |  |  |
| (b) |  | B1 <br> B1 | 2 | AWFW <br> (2.68701) <br> AWFW ( 0.0037523 or 0.0038159 ) <br> Accept ( 3.7 to 3.9 ) $\times 10^{-3}$ (see GN6) |
|  |  |  |  |  |
|  |  | Total | 6 |  |



| Q | Solution | Marks | Total | Comments |
| :---: | :---: | :---: | :---: | :---: |
| $\begin{gathered} 4 \\ (\mathrm{a}) \end{gathered}$ | Scatter diagram: $\quad \begin{array}{r}4 \text { points } \\ \\ \\ 2 \text { or } 3 \text { points }\end{array}$ | $\begin{aligned} & \text { B2 } \\ & \text { (B1) } \end{aligned}$ | 2 | Within red box on overlay (Ignore any additional points or any labelling of points) |
| (b) (i) | $\begin{aligned} b(\text { gradient } / \text { slope }) & =\underline{\mathbf{0 . 4} \text { to } \mathbf{0 . 4 1}} \\ b(\text { gradient } / \text { slope }) & =\underline{\mathbf{0 . 3 5} \text { to } \mathbf{0 . 4 5}} \\ a(\text { intercept }) & =\underline{\mathbf{1 . 2} \text { to } \mathbf{1 . 4}} \\ a \text { (intercept) } & =\underline{\mathbf{0 . 4 5} \text { to } \mathbf{2 . 3 5}} \end{aligned}$ <br> Attempt at $\sum x \sum x^{2} \quad \sum y \& \sum x y$ or <br> Attempt at $S_{x x} \& S_{x y}$ <br> Attempt at substitution into correct corresponding formula for $b$ $b=\underline{0.40} \text { to } 0.41 \quad a=\underline{1.2} \text { to } 1.4$ | B2 <br> (B1) <br> B2 <br> (B1) <br> (M1) <br> (m1) <br> (A1 A1) | (4) | AWFW <br> (0.40517) <br> AWFW <br> For answers as fractions, see Note 7 <br> AWFW <br> (1.30186) <br> AWFW <br> AWFW $(\bar{x}=19 \& \bar{y}=9)$ |
| Notes | 1 Treat rounding of correct, but not of incorrect, answers as ISW <br> 2 Written form of equation is not required <br> 3 Award 4 marks for $y=(1.2$ to 1.4$)+(0.4$ to 0.41$) x$ or for $(1.2$ to 1.4$)+(0.4$ to 0.41$) x$ <br> 4 Values of $a$ and $b$ interchanged and equation $y=a x+b$ used for drawing line $\Rightarrow$ max of 4 marks <br> 5 Values of $a$ and $b$ interchanged and equation $y=a+b x$ used for drawing line $\Rightarrow 0$ marks <br> 6 Values are not identified or simply $b / a=\#$ and $a / b=\#$, then 0.35 to $0.45 \Rightarrow \mathrm{~B} 1$ and 0.45 to $2.35 \Rightarrow$ B1 but accept, for example, as identification, $[b=\#, a=\#$ with $y=a+b x$ but no substitution for $b \& a]$ or $[$ slope $/ \operatorname{gradient}(b)=\#, \operatorname{intercept}(a)=\#]$ <br> 7 Answers in fractions can score at most B1 B1 or M1 m1 <br> 8 Some/all of marks can be scored in (b)(ii), (c) \& (d)(i), even if some/all of marks are lost in (b)(i), but marks lost in (b)(i) cannot be recouped by subsequent working in (b)(ii), (c) or (d)(i) |  |  |  |
| Notes | Scatter diagram <br> line <br> Line must be (approximately) straight; <br> not dog leg, curve or wavy | B2 | (2) | From at least $x=8$ to $x=30$ (allow a tolerance of 2 squares (ie 4 mm ) on line length) <br> and within red tolerance lines on overlay, even if drawn by eye |
|  | 1 If, and only if, B0, then award M1 for seen use of an equation for at least two points <br> 2 If, and only if, B0, then award M0 for points or line marked on scatter diagram without supportive working |  |  |  |
|  |  |  | 6 |  |
|  | Parts (a) \& (b)(i) | Total | 8 |  |


| Q | Solution | Marks | Total | Comments |
| :---: | :---: | :---: | :---: | :---: |
| 4 | Continued Parts (a) \& (b)(i) | Total | 8 |  |
| (b) <br> (ii) | $b$ : each/every/one/an additional tile takes or increase per tile is (on average) $\boldsymbol{b}$ hours $/ \mathbf{6 0 b}$ mins | $\begin{gathered} \mathrm{B} 1 \\ \mathrm{BF} 1 \end{gathered}$ | (2) | F on $b$ providing $\mathbf{0 . 3 5} \leq \boldsymbol{b} \leq \mathbf{0 . 4 5}$ and correct units are stated |
| Notes <br> SC | 1 To score any marks, an explanation must indicate change in $x$ affecting change in $y$, not change in $y$ affecting change in $x$ <br> 2 Reference only to correlation $\Rightarrow \mathrm{B} 0 \mathrm{BF} 0$ <br> 1 As $x /$ number of tiles increases then $y /$ time increases by $b / 60 b$ (OE; value of $b(0.35 \leq b \leq 0.45$ ) must be stated but context and/or units are not required) $\Rightarrow \mathrm{B} 1$ |  |  |  |
|  | $a$ : time to replace no/zero tiles, start-up time, minimum time, time for travelling, preparation, erecting ladders, obtaining materials, etc | BF1 | (1) | OE; in context <br> Reference to the value of $a$ is not required <br> F on $a$ providing $\boldsymbol{a}>\mathbf{0}$ |
|  |  |  | 3 |  |
| (c) | $y(15)=7$ to 8 | B1 | 1 | AWFW <br> From calculation/graph/guesswork Hours not required |
| Note | 1 Accept (420 to 480) minutes only if "minutes/mins" are stated |  |  |  |
| (d) <br> (i) | $\begin{aligned} & \begin{array}{l} r_{6}=8.8-a-b \times 20 \\ r_{6} \end{array}= \\ &=\underline{\mathbf{0 . 6} \text { to }-\mathbf{0 . 6 1}} \\ & \mathbf{0 . 5} \text { to } \mathbf{0 . 7} \end{aligned}$ | $\begin{aligned} & \mathrm{B} 2 \\ & (\mathrm{~B} 1) \end{aligned}$ | 2 | AWFW; do not ignore sign ( -0.60517 ) <br> AWFW; ignore sign |
| Note | 1 If , and only if, B0, then attempted use of $\pm(8.8-a-b \times 20) \Rightarrow$ M1 providing $0.35 \leq b \leq 0.45$ and $0.45 \leq a \leq 2.35$ |  |  |  |
|  | Value will be/is always: <br> 0 or zero or nought or nothing | B1 | 1 | CAO; accept nothing else, but ignore zeros after decimal point (eg 0.00) Ignore any explanation |
|  |  | Total | 15 |  |


| Q | Solution | Marks | Total | Comments |
| :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | Accept percentage equivalent answers in (a) but see GN4 |
| (a)(i) | $\begin{aligned} & \mathrm{P}(X<1.9)=\mathrm{P}\left(Z<\frac{1.9-1.81}{0.08}\right) \\ &=\mathrm{P}(Z<1.125)=\underline{\mathbf{0 . 8 7}} \end{aligned}$ | M1 <br> A1 | (2) | Standardising 1.9 with 1.81 and 0.08 but allow (1.81-1.9) <br> AWRT (0.86971) |
| (ii) | $\begin{aligned} \mathrm{P}(X>1.85)=\mathrm{P}(Z>0.5) & =1-\mathrm{P}(Z<0.5) \\ & =1-0.69146=\underline{\mathbf{0 . 3 1}} \end{aligned}$ | M1 <br> A1 | (2) | Area change; can be implied by any final answer $<0.5$ <br> AWRT <br> (0.30854) |
| (iii) | $\begin{aligned} & \mathrm{P}(1.81<X<1.85) \\ & \text { or }=(0.691 \text { to } 0.692)-0.5 \\ &=0.5-(0.308 \text { to } 0.309) \\ &=\underline{\mathbf{0 . 1 9} 9} \end{aligned}$ | B1 <br> B1 | (2) | Can be implied by a correct answer <br> AWRT <br> (0.19146) |
|  |  |  | 6 |  |
| (b)(i) | $\begin{array}{r} z=\text { or }<\frac{9.25-\mu}{\sigma} \text { or } 9.25=\mu+z \sigma \\ 0.88 \Rightarrow z=\underline{\mathbf{1 . 1 7} \text { to } \mathbf{1 . 1 8}} \tag{1.175} \end{array}$ | M1 <br> B1 | 2 | Either expression or with $z$ replaced by 1.17 to 1.18 (AWFW) <br> AWFW (ignore sign) |
| Notes | 1 Allow $\bar{x} /$ mean instead of $\mu$ and/or $s /$ sd instead of $\sigma$ 2 Result of $9.25-\mu=z \sigma$ stated without any prior eviden 3 Working back from the given answer $9.25-\mu=z \times \sigma$ <br> 4 The M1 cannot be scored for work in (b)(ii) <br> 5 The $z$-value of 1.17 to 1.18 (AWFW) must be seen in (b) | $\begin{aligned} & e \Rightarrow \mathrm{M} 0 \\ & \Rightarrow \mathrm{M} 0 \end{aligned}$ <br> i) to score | seen | aly in (b)(ii) scores B0 |
| (ii) | Thus$\mathrm{P}(Y>8.75)$ $=0.975 \Rightarrow z=\underline{\mathbf{1 . 9 6}}$ <br>  $9.25-\mu$ $=+1.175 \sigma$ <br> $8.75-\mu$ $=-1.96 \sigma$ <br> giving $0.5=3.135 \sigma$ | B1 <br> M1 <br> Adep1 <br> Adep1 | 4 | AWRT (ignore sign) <br> (1.17 to 1.18) AWFW (ignore sign) (1.96) AWRT (ignore sign) A valid method for solution of two equations that are correct except for signs of $z$-values (see Note 1) <br> AWRT <br> (0.15949) <br> Dependent on two fully correct equations including signs of $z$-values <br> AWFW <br> (9.06260) |
| Note | 1 Accept method as shown or substitution for either $\mu$ or $\sigma$ from one equation into the other, even if $z$-value signs are incorrect |  |  |  |
|  |  |  |  |  |
|  |  | Total | 12 |  |


| Q | Solution | Marks | Total | Comments |
| :---: | :---: | :---: | :---: | :---: |
| 6 <br> (a) <br> (i) | Accept 3 dp rounding of probabilities from tables |  |  | Accept percentage equivalent answers in <br> (a) \& (b) but see GN4 |
|  | $\mathrm{P}(X \leq 15) \quad=\underline{0.694}$ to 0.695 | B1 | (1) | AWFW (0.6946) |
| (ii) <br>  <br>  <br> Note | $\begin{aligned} \mathrm{P}(X>10) & =1-0.1215 \\ & =\underline{\mathbf{0 . 8 7 8} \text { to } \mathbf{0 . 8 7 9}} \\ & =1-0.0644 \text { or } 0.935 \text { to } 0.936 \end{aligned}$ | M1 <br> A1 <br> (M1) | (2) | AWFW (0.8785) |
|  | 1 For calculation of individual terms or no method: award B2 for 0.878 to 0.879 (AWFW); B1 for 0.935 to 0.936 (AWFW) |  |  |  |
| (iii) | $\begin{aligned} \mathrm{P}(12<X & <18) \\ & \left(p_{1}\right) \\ & \\ & \left(p_{2}\right) \\ 0.8761 & \text { or } \end{aligned} 0.9301$ <br> MINUS 0.3143 or 0.2053 $=\underline{0.561} \text { to } 0.562$ | M1 <br> M1 <br> A1 | (3) | AWFW (0.5618) |
| Notes | 1 For calculation of individual terms or no method: award B3 for 0.561 to 0.562 (AWFW); B2 for 0.670 to 0.671 (AWFW); B2 for 0.615 to 0.616 (AWFW); B2 for 0.724 to 0.725 (AWFW) $2\left(1-p_{2}\right)-\left(1-p_{1}\right) \Rightarrow$ M1 M1 A1 or M1 M1 or M1 |  |  |  |
| (iv) | $\begin{aligned} & \text { Mean of distribution }=40 \times 0.35=\underline{\mathbf{1 4}} \\ & \mathrm{P}(X=14) \\ & \text { or } \\ & =\binom{40}{14} 0.35^{14} 0.65^{26} \\ & =0.5721-0.4408 \\ & =\underline{\mathbf{0 . 1 3 1} \text { to } \mathbf{0 . 1 3 2}} \end{aligned}$ | B1 <br> M1 <br> A1 | (3) | CAO; can be implied <br> Fully correct expression <br> Can be implied <br> Correct difference <br> AWFW <br> (0.1313) |
|  |  |  | 9 |  |
| Note | Selection is at random $\begin{aligned} & \mathrm{P}(Y<30 \mid \mathrm{B}(50,0.7)) \\ &=1-0.9522 \\ &=\underline{\mathbf{0 . 0 4 7} \text { to } \mathbf{0 . 0 4 8}} \\ &=1-0.9152 \text { or } 0.084 \text { to } 0.085 \\ &=1-0.9749 \end{aligned} \begin{aligned} & \text { or } 0.025 \text { to } 0.026 \\ & \\ & \\ & \end{aligned} \quad 0.952 \text { to } 0.953 .$ | B1 <br> M2 <br> A1 <br> (M2) <br> (M2) <br> (M1) | 4 | Statement must include word "random" <br> AWFW <br> (0.0478) |
|  | 1 For direct use of $\mathrm{P}(Y<30 \mid \mathrm{B}(50,0.7))$ using calculator or no method: award (B1) B3 for 0.047 to 0.048 (AWFW); <br> (B1) B2 for 0.084 to 0.085 (AWFW); (B1) B2 for 0.025 to 0.026 (AWFW); (B1) M1 for 0.952 to 0.953 |  |  |  |
|  |  |  |  |  |
|  |  | Total | 13 |  |



\begin{tabular}{|c|c|c|c|c|}
\hline Q \& Solution \& Marks \& Total \& Comments \\
\hline 7 \& Continued \& \& \& \\
\hline \& Part (a) \& Total \& 4 \& \\
\hline (b)
(i) \&  \& \begin{tabular}{l}
M2,1 \\
( -1 ee) \\
Adep 1
\end{tabular} \& \(\sqrt{\sqrt{2}}\) \& \begin{tabular}{l}
AWFW \\
(2.5758) \\
AWFW \\
Ignore any notation \\
M0 if CI is not of the form:
\[
\begin{aligned}
\& \bar{x} \pm z \times \frac{\sigma}{\sqrt{40 \text { or } 39}} \\
\& 5.37 \times \sqrt{\frac{40}{39}}=5.4384
\end{aligned}
\] \\
CAO; note 'or' (not 'to') \\
Dependent on award of M2 \\
CAO; note 'or'
\end{tabular} \\
\hline Note \& \multicolumn{4}{|l|}{\(\mathbf{1}\) An incorrect expression for CI followed by a numerically correct \(\mathrm{CI} \Rightarrow 2\) solutions \(\Rightarrow((0\) or 1\()+4) / 2 \Rightarrow 2\) marks} \\
\hline \multirow{3}{*}{Notes} \& \begin{tabular}{l}
Claim 1: \\
Clear correct comparison of \(\mathbf{3 0 0}\) with CI eg 300 is below CI or LCL \(>300\) \\
Agree with or accept claim
\end{tabular} \& \begin{tabular}{l}
BF1 \\
Bdep1
\end{tabular} \& (2) \& \begin{tabular}{l}
Statement must include reference to 300 \\
F on CI providing it is above 300 Must have found an interval in (b)(i) but quoting values for CI or CLs is not required \\
OE ; dependent on BF1
\end{tabular} \\
\hline \& \multicolumn{4}{|l|}{```
1 Statement must clearly indicate that " 300 is below the C1" OE
Statements of the form "It/mean/value/etc is below/outside/not within the CI" \(\Rightarrow \mathrm{BF} 0\)
Statements of the form " 300 is below/outside/not within \(99 \%\) of the data/values/weights" \(\Rightarrow\) BF0
Statements such as "Claim is likely/reasonable/supported/correct/true/possible/valid" \(\Rightarrow\) Bdep1 providing BF1
```} \\
\hline \& \begin{tabular}{l}
Claim 2: \\
Attempt at \\
304.6 - 5.37n \\
Result \(<\mathbf{3 0 0}\) so \\
disagree with or reject claim
\end{tabular} \& M1

A1 \& (2) \& | Allow $0.86 \leq n \leq 3$ with a correct numerical answer (see Note 1) |
| :--- |
| OE |
| Must be a clear correct comparison of stated 300 with calculated result | <br>

\hline Notes \& \multicolumn{4}{|l|}{} <br>
\hline \& \& \& 4 \& <br>
\hline \& \& \& \& <br>
\hline \& \& \& 12 \& <br>
\hline
\end{tabular}


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